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# Validity of summary statistics-based mixed-effects group fMRI

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## Introduction

Statistical analysis of multi-subject functional Magnetic Resonance Imaging (fMRI) data is traditionally done using either: 1) a mixed-effects GLM (MFX GLM) where within-subject variance estimates are used and incorporated into per-subject weights or 2) a random-effects General linear model (GLM) (RFX GLM) where within-subject variance estimates are not used. Both approaches are implemented and available in major neuroimaging software packages including: SPM (MFX analysis; 2nd-Level statistics), FSL (FLAME; OLS) and AFNI (3dMEMA; 3dttest++). While MFX GLM provides the most efficient statistical estimate, its properties are only guaranteed in large samples, and it has been shown that RFX GLM is a valid alternative for one-sample group analyses in fMRI [1]. We recently showed that MFX GLM for image-based meta-analysis could lead to invalid results in small-samples. Here, we investigate whether this issue also affects group fMRI.

## Methods

GLM can be expressed with:  $Y = X\beta + \epsilon$ , where  $Y$  is the  $N$ -vector of subject-level contrast estimates,  $X$  the design matrix,  $\beta$  the group parameter to estimate and  $\epsilon$  the random error. In group fMRI, the error term has two contributions, from within- and between-subject variance.

**MFX GLM.** Using within-subject variance estimates requires a weighted least squares (WLS) approach, where the group parameter  $\beta$  is a weighted average of the subject-level contrasts. The weights are inversely proportional to the sum of the within- and between-subject variances. But in practice, those weights are unknown and have to be estimated from the data leading to a Feasible Generalised Least Squares (FGLS). FGLS is asymptotically efficient but its finite sample properties are unknown [2]. We used FSL's 'FLAME 1' FGLS that uses maximum likelihood to estimate between-subject variance, computing a T-statistic compared to a Student distribution with  $N-1$  degrees of freedom (DF) [3].

**RFX GLM.** Under the assumption that the within-subject variance is constant or negligible in comparison to the between-study variance, the weights above are equal and the GLM can be estimated with Ordinary Least Squares (OLS),  $\beta$  estimated as the average of the subject-level contrasts. We used SPM's 2nd level one-sample model, computing a T statistic also compared to a Student distribution with  $N-1$  DF [4]. OLS p-values are exact for any sample size, in contrast to FGLS which are only asymptotically valid [2].

We used Monte Carlo simulations to investigate the validity of MFX and RFX GLMs under varying degrees of within-subject variance heteroscedasticity. Within-subject variances took on 2 values, a 'good' value and a 'high' values of 2, 4, 8 & 16x good values; we considered 4%, 20%, 40%, 80% or 96% of the subjects to have the high values. We fixed the mean within-subject standard error to be equal to the between-subject variance. We assumed 25 subjects per group and 1000 independent time points per subject. Accuracy was assessed by comparing FSL & SPM distributions of  $-\log_{10}$  P-values to Monte Carlo  $-\log_{10}$  P-values based on  $10^6$  realisations.

## Results

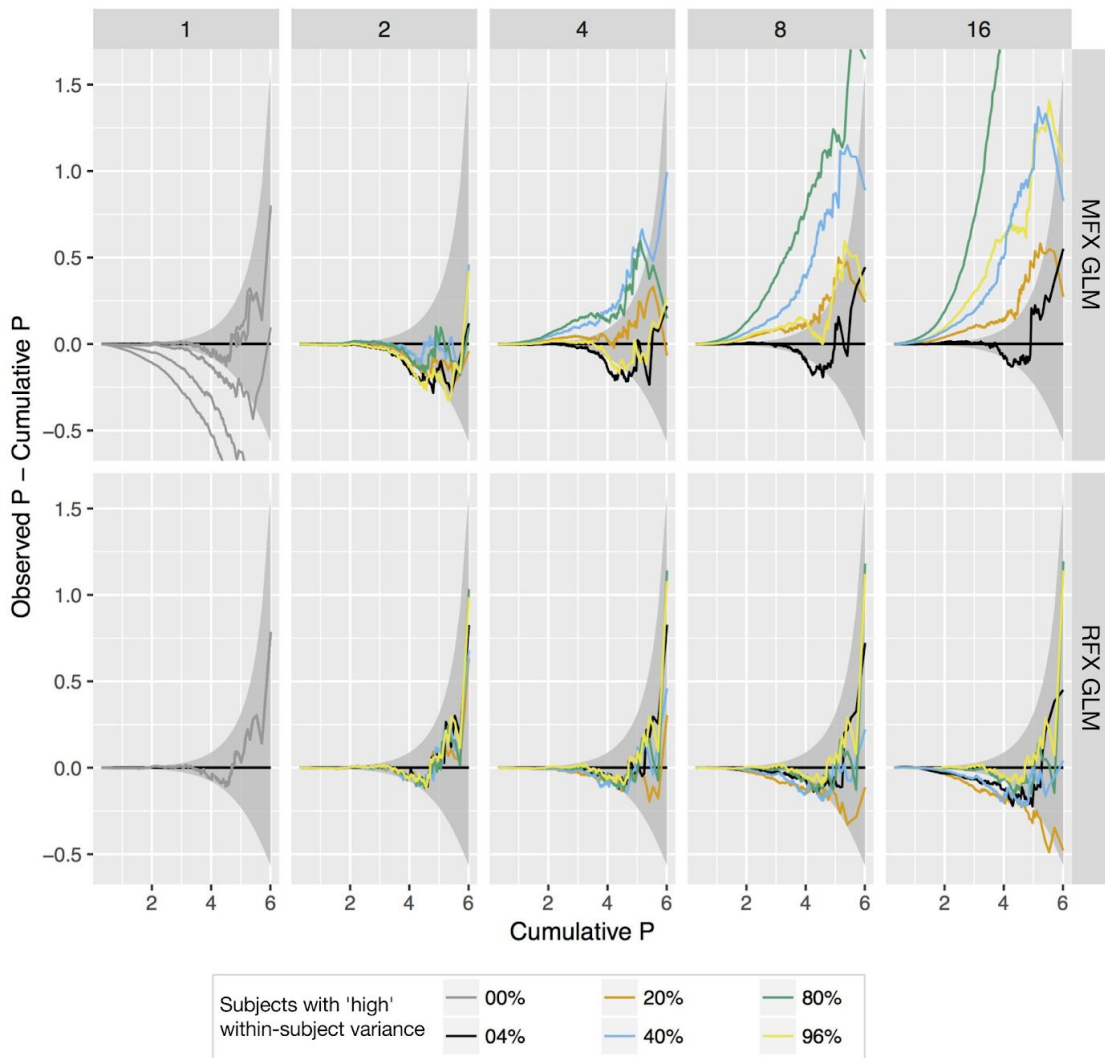
Fig. 1 presents deviation from theoretical P-values with varying percentage and intensity of high intra-subject variance. For low intensity heteroscedasticity ( $\leq 2x$ ), MFX GLM is valid but becomes increasingly invalid in the presence strong and prevalent high variance subjects. RFX GLM is valid with all settings but displays some conservativeness in the presence of strong heteroscedasticity.

## Conclusions

Here we investigated the validity of RFX and MFX GLMs in the presence of varying within-subject variance. As previously shown in the literature [1], we observed that RFX GLM is robust to the presence of heteroscedasticity. More surprisingly, MFX GLM was invalid in the presence of high variations in within-subject variances. More work is needed to investigate which of these settings is closest to the patterns present in real fMRI data. In the meantime, we recommend RFX GLM when working with small samples.

## Figures

## Validity of group-level fMRI models in small samples



**Fig. 1.** Deviation of observed from theoretical P-values (difference of observed and Monte Carlo ('true')  $-\log_{10}$  p-value distributions) for one-sample tests in the presence of varying percentages of subjects with outlying within-subject variances, high-variance factor 2, 4, 8 or 16, (columns), MFX GLM and RFX GLM (rows). Y-axis is the observed cumulative probability minus Monte Carlo cumulative probability for a given (X-axis)  $-\log_{10}$  p-value; positive deflections correspond to inflated false positive risk.

**Fig. 1.** Deviation of observed from theoretical P-values (difference of observed and Monte Carlo ('true')  $-\log_{10}$  p-value distributions) for one-sample tests in the presence of varying percentages of subjects with outlying within-subject variances, high-variance factor 2, 4, 8 or 16, (columns), MFX GLM and RFX GLM (rows). Y-axis is the observed cumulative probability minus Monte Carlo cumulative probability for a given (X-axis)  $-\log_{10}$  p-value; positive deflections correspond to inflated false positive risk.

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