

### Additional file 1 — Calculation of the parameters of the different censoring mechanisms.

The censoring mechanism was assumed to be independent uniform  $C_i \sim \mathcal{U}\{0, r\}$  or exponential  $C_i \sim \mathcal{E}(\gamma)$ .

- For a Cox proportional hazards model, the survival function was exponential with parameters  $\lambda = \lambda_0 e^{\beta Z}$ .

In order to determine  $r$  and  $\gamma$  for a given value of the expected overall percentage  $p_c$  of censoring, we solved iteratively for  $r_p$  and  $\gamma_p$  (value of  $r$  and  $\gamma$  for a given percentage of censoring  $p_c$ , respectively) in the following equations.

Under the null hypothesis ( $\beta = 0$ ), the equations to solve were

$$p_c = \frac{1}{\lambda_0 r_p} (1 - e^{-\lambda_0 r_p}) , \text{ for a uniform censoring}$$

and

$$p_c = \frac{\gamma_p}{\lambda_0 + \gamma_p} , \text{ for an exponential censoring}$$

Under the alternative hypothesis (i.e. with covariate,  $\beta \neq 0$ ), the equations to solve were

$$p_c = \int_{\mathcal{R}} \left\{ \frac{1}{r_p \lambda_0 \exp(\beta z)} (1 - e^{-\lambda_0 r_p \exp(\beta z)}) f_Z(z) \right\} dz$$

for a uniform censoring, and

$$p_c = \int_{\mathcal{R}} \left\{ \frac{\gamma_p}{\gamma_p + \lambda_0 \exp(\beta z)} f_Z(z) \right\} dz$$

for an exponential censoring. The function  $f_Z(z)$  denote the density of the covariate  $Z$ .

- Under a proportional odds model,  $T$  had a log-logistic distribution with density  $f(t) = \lambda_0 e^{-\beta z} / (1 + t e^{-\beta z})^2$ . In this case, the equations to solve under the null hypothesis were

$$p_c = \frac{\ln(r)}{r} , \text{ for a uniform censoring}$$

and

$$p_c = \int_0^\infty \frac{\gamma e^{-\gamma c}}{1 + c} dc , \text{ for an exponential censoring}$$

Under the alternative hypothesis, the equations were

$$p_c = \int_{\mathcal{R}} \left\{ \frac{\ln(1 + r e^{-\beta z})}{r} f_Z(z) \right\} dz$$

for a uniform censoring, and

$$p_c = \int_{\mathcal{R}} \left\{ \int_0^\infty \left( \frac{\gamma e^{-\gamma c}}{1 + c e^{-\beta z}} \right) dc \right\} f_Z(z) dz$$

for an exponential censoring.

- For both models, for one subject  $i$  and for a uniform censoring, two independent uniform variates  $U_{0.25}^i$  and  $U_{0.5}^i$  on  $\{0, r_{0.25}^i\}$  and  $\{0, r_{0.5}^i\}$  were generated, respectively. For an exponential censoring, two independent exponential variates  $\mathcal{E}_{0.25}^i$  and  $\mathcal{E}_{0.5}^i$  with parameters  $\gamma_{0.25}^i$  and  $\gamma_{0.5}^i$  were generated, respectively. In both cases, the three variates  $T^i$ ,  $\min(T^i, C_{0.25}^i)$  and  $\min(T^i, C_{0.5}^i)$ , with  $C^i = U^i$  or  $\mathcal{E}^i$ , represent the observed times for the subject  $i$  in three situations with an expected percentage of censoring equal to 0, 25 and 50%, respectively.