

A model of the guinea-pig ventricular cardiac myocyte incorporating a transverse-axial tubular system

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Appendix 2

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Fig. 6A represents the simplified equivalent electrical circuit of the cardiac cell connected to the voltage source (V_c) through electrode resistance R_{el} , including the transverse-axial tubular system (TATS). It is applicable for small (sub-threshold) voltage variations around resting membrane voltage. C_s and C_t are the capacitance, and R_{ms} and R_{mt} the resistance, of the surface and tubular membranes, respectively. V_{ms} and V_{mt} are membrane voltages. R_{st} stands for luminal resistance in a single-compartment approximation.

The circuit is described by a set of two differential equations

$$\frac{dV_{\text{ms}}}{dt} = a_{11} V_{\text{ms}} + a_{12} V_{\text{mt}} + \frac{V_{\text{c}}}{R_{\text{el}} C_{\text{s}}}, \quad \frac{dV_{\text{mt}}}{dt} = a_{21} V_{\text{ms}} + a_{22} V_{\text{mt}}$$
(1)

where

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$$a_{11} = -\frac{1}{C_s} \left(\frac{1}{R_{el}} + \frac{1}{R_{st}} + \frac{1}{R_{ms}} \right), \ a_{12} = \frac{1}{C_s R_{st}}, \ a_{21} = \frac{1}{C_t R_{st}}, \ a_{22} = -\frac{1}{C_t} \left(\frac{1}{R_{st}} + \frac{1}{R_{mt}} \right). \tag{2}$$

For measurement of membrane capacitance from the current responses to a small voltage step, membrane voltage V_c is constant and solution of equations (1) is expressed as a sum of two exponential functions and a constant

$$V_{\rm ms} = V_{\rm s1} e^{-\frac{t}{\tau_1}} + V_{\rm s2} e^{-\frac{t}{\tau_2}} + V_{\rm s0}, \quad V_{\rm mt} = V_{\rm t1} e^{-\frac{t}{\tau_1}} + V_{\rm t2} e^{-\frac{t}{\tau_2}} + V_{\rm t0}. \tag{3}$$

The time constants τ_1 and τ_2 are obtained from the roots (λ_1, λ_2) of characteristic equation

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$$\lambda^2 - \lambda (a_{11} + a_{22}) + a_{11}a_{22} - a_{12}a_{21} = 0$$

as

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$$\tau_{1} = -\frac{1}{\lambda_{1}} = \frac{-2}{a_{11} + a_{22} + \sqrt{(a_{11} - a_{22})^{2} + 4a_{12}a_{21}}},$$

$$\tau_{2} = -\frac{1}{\lambda_{2}} = \frac{-2}{a_{11} + a_{22} - \sqrt{(a_{11} - a_{22})^{2} + 4a_{12}a_{21}}}.$$
(4)

The constants $V_{\rm s0}$ and $V_{\rm t0}$ depend only on the circuit resistances

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$$V_{s0} = V_{c} \frac{R_{ms} (R_{st} + R_{mt})}{R_{ms} (R_{st} + R_{mt}) + R_{cl} (R_{st} + R_{mt} + R_{ms})}, \quad V_{t0} = V_{s0} \frac{R_{mt}}{R_{mt} + R_{st}}.$$
 (5)

Assuming initial conditions $V_{\rm ms}=0$, $V_{\rm mt}=0$ and taking into account (2), (4) and (5), the magnitudes of exponential components can be calculated as

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$$V_{\rm sl} = \frac{1}{A} \left[V_{\rm s0} a_{21} a_{12} + V_{\rm t0} \left(a_{22} a_{12} - a_{12} \lambda_2 \right) \right],$$

$$V_{s2} = \frac{1}{A} \left[V_{s0} a_{11} (\lambda_2 - a_{22}) + V_{s0} \lambda_1 (a_{22} - \lambda_2) + V_{t0} a_{12} (\lambda_2 - a_{22}) \right],$$

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$$V_{t1} = \frac{1}{4} \left[-V_{s0} a_{21} (a_{11} - \lambda_1) + V_{t0} (\lambda_2 - a_{22}) (a_{11} - \lambda_1) \right], \tag{6}$$

$$V_{t2} = \frac{1}{A} \left[V_{s0} \left(a_{21} a_{11} - a_{21} \lambda_1 \right) + V_{t0} a_{21} a_{12} \right].$$

where

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$$A = -a_{21}a_{12} + a_{22}a_{11} - a_{11}\lambda_2 - a_{22}\lambda_1 + \lambda_1\lambda_2.$$

The solution of equation (1) allows us to express the response of membrane current $(I_{\rm m})$ to an imposed voltage step from resting voltage (regarded as zero voltage) to the level $V_{\rm c}$ considering the relation $I_{\rm m} = (V_{\rm c} - V_{\rm ms})/R_{\rm el}$.

$$I_{\rm m} = I_1 e^{-\frac{t}{\tau_1}} + I_2 e^{-\frac{t}{\tau_2}} + I_0 , \qquad (7)$$

where

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$$I_{1} = -\frac{V_{\rm s1}}{R_{\rm el}}, \quad I_{2} = -\frac{V_{\rm s2}}{R_{\rm el}}, \quad I_{0} = \frac{V_{\rm c} - V_{\rm s0}}{R_{\rm el}}.$$

If numeric values of passive electrical parameters adopted for our model cardiac cell are inserted into (6) and (7), the second exponential terms of V_s , V_t , and I_m related to the short time constant ($\tau_2 \sim 1 \mu s$) become negligible (in contrast to the situation in skeletal muscle cells). The time constant τ_1 of the dominant component approaches the value corresponding to the limit conditions ($R_{st} \rightarrow 0$, $R_{ms} \rightarrow \infty$, $R_{st} \rightarrow \infty$) under which the cell would respond to small voltage steps by processes following single exponential course with time constant $\tau = R_{el}$ ($C_s + C_t$).